

or

$$K(x, p) = \frac{a^{ij}(x)p_i p_j}{b^i(x)p_i} \quad (5)$$

with  $a_{ij}a^{jk} = \delta_i^k$  and we will again call these spaces Randers and, respectively, Kropina spaces on the cotangent bundle  $T^*M$ .

*([8])*

Let  $L(x, y)$  be a regular Lagrangian on a domain  $D \subset TM$  and let  $H(x, p)$  be a regular Hamiltonian on a domain  $D^* \subset T^*M$ .

*It is known that*

As we know ([8]) if  $L$  is a differentiable map, we can consider the fiber derivative of  $L$ , locally given by the diffeomorphism between the open set  $U \subset D$  and  $U^* \subset D^*$ :

$$\varphi(x, y) = (x^i, \dot{\partial}_a L(x, y)) \quad (6)$$

which is called the Legendre transformation. We can define, in this case, the function  $H : U^* \rightarrow R$ :

$$H(x, p) = p_a y^a - L(x, y), \quad (7)$$

where  $y = (y^a)$  is the solution of the equations:

$$p_a = \dot{\partial}_a L(x, y). \quad (8)$$

In the same manner, the fiber derivative is given locally by:

$$\psi(x, p) = (x^i, \partial^a H(x, p)), \quad (9)$$

*the function*

$\psi$  is a diffeomorphism between the same open sets  $U^* \subset D^*$  and  $U \subset D$  and we can consider the function  $L : U \rightarrow R$ :

$$L(x, y) = p_a y^a - H(x, p), \quad (10)$$

where  $p = (p_a)$  is the solution of the equations:

$$y^a = \partial^a H(x, p). \quad (11)$$

The Hamiltonian given by (7) is called the Legendre transformation of the Lagrangian  $L$  and the Lagrangian given by (10) is called the Legendre transformation of the Hamiltonian  $H$ .

*puneti \$L\$  
\$H\$  
([8])*

If  $(M, K)$  is a Cartan space, then  $(M, H)$  is a Hamilton manifold [8] where  $H(x, p) = \frac{1}{2}K^2(x, p)$  is 2-homogenous on a domain of  $T^*M$ . So, we get the following transformation of  $H$  on  $U$ :

$$L(x, y) = p_a y^a - H(x, p) = H(x, p). \quad (12)$$

**Proposition 1.1** ([8]) The scalar field  $L(x, y)$  defined by (12) is a positively 2-homogeneous regular Lagrangian on  $U$ .

Therefore, we get Finsler metric  $F$  of  $U$ , so that

*puneti prop  
in citat  
{cit ...}*

$$L = \frac{1}{2}F^2 \quad (13)$$

*and like  
dupa prop.*

*Puneti testele tutoror Theoremelor, Lemelor, Propozitiilor, etc  
in citat {cit ...}*